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METEOROLOGICAL DATA ON FIELD. (U) ARMY ELECTRONICS
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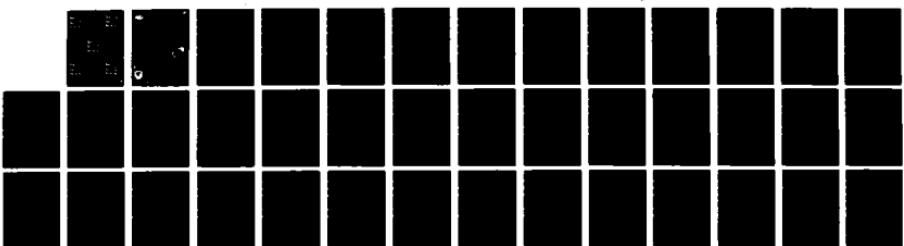
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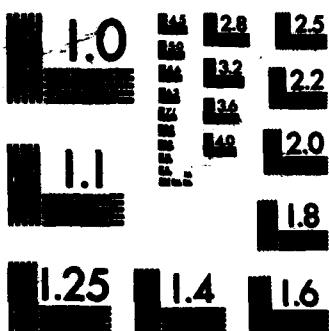
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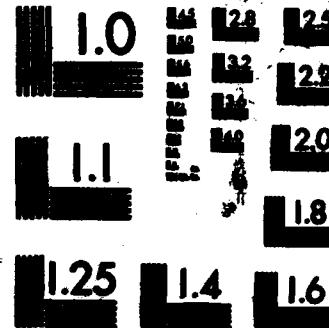


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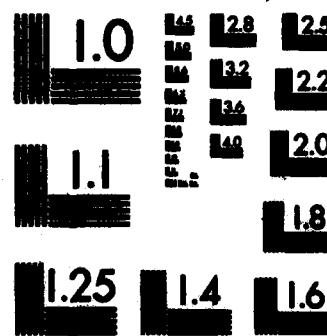
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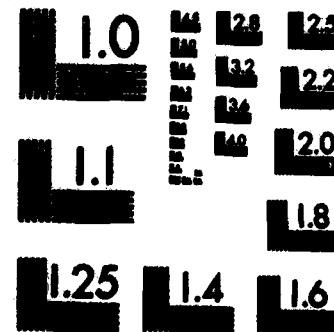
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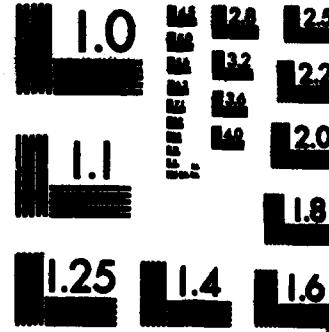
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IMPACT OF SPACIAL AND TEMPORAL FREQUENCY OF METEOROLOGICAL
DATA ON FIELD ARTILLERY ACCURACY

AUGUST 1982

By
J. D. Copp

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US Army Electronics Research and Development Command
Atmospheric Sciences Laboratory

White Sands Missile Range, NM 88002

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The effect of spacial and temporal frequency of radiosonde data on artillery accuracy is analyzed for the 8-in (short tube) and 155 mm (long tube) weapon systems. Range and deflection elliptical probable errors for hitting a stationary target are calculated for various firing scenarios using real meteorological data from central Europe. The individual errors due to variability and uncertainty in wind, temperature, and density measurements are also analyzed for several of the firing examples.		

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The author wishes to thank Dr. D. M. Swingle for developing the equations which were used to generate the elliptical probable errors for this study.

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INTRODUCTION

The effects of wind, temperature, and density on a projectile are easy to understand. Acquiring the necessary meteorological (met) data so corrections can be applied before firing the projectile, however, is easier to talk about than to do. Often a weapon will be fired using a met message several hours old, or a projectile will be fired in a direction opposite to that which the radiosonde balloon was carried by the prevailing wind. Because the balloon and projectile will never be at the same place at the same time, the met message will always be stale. Also, no radiosonde and angular tracking system is completely free of measurement error. Thus we will always be firing a projectile using met data that is not entirely correct for the current time and location. The purpose of this study is to show in a statistical manner how range and deflection probable errors increase due to space-time staleness and to measurement uncertainty of the ballistic met message parameters. The probable errors generated for this study were attained using equations developed by Swingle* that describe the variability and measurement errors of the ballistic met message parameters.

DISCUSSION

There are four basic types of met error that will affect the range accuracy of a field artillery weapon. These errors are (1) time and space variability of ballistic wind, (2) measurement uncertainty of ballistic wind, (3) time and space variability of ballistic temperature and density, and (4) measurement uncertainty of ballistic temperature and density. Because of the relationship between temperature and density, as seen by the equation of state, it is necessary to compute the combined effect of their variations.

All of the above individual errors in the met data will be expressed as variances for the range and deflection components of trajectory. The sum of the range and deflection variances then can be converted to standard deviations and finally to elliptical probable errors of the range and deflection estimate. Expressing the total range and deflection variances in equation form:

$$X^2 = ST \cdot RWV + RWM + ST \cdot RTDV + RTDM \quad (1)$$

$$Y^2 = ST \cdot DWV + DWM \quad (2)$$

*Swingle, D. M., unpublished work, US Army Atmospheric Sciences Laboratory, White Sands Missile Range, NM, 1979.

where

X^2 = total range variance (m^2)

Y^2 = total deflection variance (m^2)

ST = space-time staleness factor (min)

RVW = range impact variance due to wind variability (m^2/min)

RWM = range impact variance due to wind measurement error (m^2)

RTDV = range impact variance due to temperature and density variability (m^2/min)

RTDM = range impact variance due to temperature and density measurement error (m^2)

DVW = deflection impact variance due to wind variability (m^2/min)

DWM = deflection impact variance due to wind measurement error (m^2).

Note that the temperature and density contributions to the deflection component of error have been dropped since they are negligible compared to the wind effects.

Many studies^{1 2 3} of wind variability in the last 30 years have focused on finding how the wind vector at a point varied in time or how the wind vector varied from point to point in space at the same instant in time. Studies⁴ have also been conducted to relate wind temporal and spacial variability. The space-time relation of parameter variability is important to this study since we want to show how accuracy of the weapon system is affected by spacial as well as temporal staleness of the ballistic met message. Since a simple scaling factor is used to equate spacial and temporal variation, the spacial staleness of the met message due to the separation between the radiosonde and the projectile can be expressed as a staleness in time. The wind studies⁵ at

¹Lowenthal, M., and R. Bellucci, "Variability of Ballistic Winds," ECOM-3529, US Army Electronics Command, Fort Monmouth, NJ, 1970.

²Durst, C. S., "The Variation of Wind With Time and Distance," Geophysical Memoir No 93, UK Meteorological Office, 1954.

³"Exercise Summerwind in the Meppen Area (West Germany)," Met Working Paper No 1, NATO Report, 4-20 July 1966.

⁴"Report on Exercise Summerwind by Denmark and the Netherlands," Met Working Paper No 85, NATO Report, 1971.

⁵Arnold, A., and R. Bellucci, "Variability of Ballistic Meteorological Parameters," Tech Memo M-1913, US Army Signal Corps Engineering Laboratories, Fort Monmouth, NJ, 1957.

Meppen, West Germany, indicate an equivalence in ballistic wind variability between 1 h in time and 30 km in distance. This can be simplified to a 2-min time interval being equivalent to a spacial separation of 1 km. This scaling factor will certainly vary some from day to day and from location to location, but the value of the 2 min/km will be used for this study since it was obtained in the NATO area and is comparable in magnitude to the results found by others.⁶

We can now define the total space-time factor, used in equations (1) and (2), representing the total space and time age of the met information.

$$ST = 2 \cdot S + T \quad (3)$$

where

S = the separation of balloon and projectile when both are at the projectile's maximum trajectory ordinate (km)

T = the time interval between the measurement of the met data and the firing of the artillery weapon (min)

The factor 2 which multiplies S is the scaling factor in min/km that relates space to time variation. The variability in windspeed due to a separation of 1 km in space between points, then, is approximately equivalent to the variability during a 2-min time interval at a single point.

In the above expression, T is the time between measurement of the met parameter and the firing of the weapon by the artilleryman. The actual measurement of wind, temperature, and density is made throughout the layer from the ground up to whichever ballistic line the projectile will reach. Depending on the thickness of the layer, the balloon could take 10, 20 or more minutes to reach the altitude of the desired ballistic line. A question arises, then, as to which point in time we take as the time of measurement. For this study it was assumed that the measurement time occurs when the radiosonde balloon reaches the altitude that corresponds to the midpoint or maximum ordinate of the projectile trajectory. Factors contributing to the time staleness of the met data are time spent tracking the balloon above the ballistic line of interest, computation of the ballistic met message, lag before broadcast of the met message, and the lag between broadcast time and firing time.

A number of factors will affect the spacial staleness, S , in equation (3), also. These factors include relative position of met station and weapon,

⁶Engebos, Bernard F., "A Least Squares Approach to Missing Meteorological Data," ASL-CR-82-0008-1, US Army Atmospheric Sciences Laboratory, White Sands Missile Range, NM, 1982.

firing direction of the weapon, balloon ascent rate, ballistic line the projectile will reach, and often, most importantly, the speed and direction of the wind. Although spacial staleness is improved when the balloon path and projectile trajectory are close, space staleness can be quite large when the firing direction is opposite that of the mean wind and drift of the radiosonde.

A brief explanation concerning the calculation of terms in equations (1) and (2) is included to further clarify the text.

1. The impact variance due to wind variability is found by multiplying the coefficient of ballistic wind variability* (kn^2/min) times the space-time factor (min) times the square of the unit effect of a range or deflection wind (m^2/kn^2). (Unit effects were obtained from the proper firing tables).⁷

2. The temperature and density variability term in equation (1) is found by multiplying the combined error per unit staleness due to temperature and density variability* (m^2/min) times the space-time factor (min).

3. The combined variance due to temperature and density measurement uncertainty was computed using a lengthy equation* involving temperature and density random and bias measurement errors.

4. Impact variances due to wind measurement were calculated by multiplying the ballistic wind component measurement variance* (kn^2) times the square of the unit effect of a range or deflection wind (m^2/kn^2).

These ballistic wind component measurement variances, for an AN/GMD-1 tracking system, were calculated by Swingle* for balloon ascent rates of 300 m/min, 400 m/min, and 500 m/min. This variance includes the error in balloon height measurement as well as balloon tracking error. There is quite a difference in these variances depending on balloon ascent rate and the ballistic line number. Table 1 lists these error variances for each balloon ascent rate. The major source of the error from the tracking system arises from angular errors because of ground reflections of the radiosonde signals. The tracking error is a function of balloon elevation angle and is less serious for a fast rising balloon than for a slower rising balloon.

With the appropriate information at hand, the total range and deflection impact variances given by equations (1) and (2) can now be calculated. Taking the square root of the variance yields the standard deviation, and multiplication by the constant factor* 1.1774 converts the standard deviation to the elliptical probable error of the range and deflection estimate. These range and deflection probable errors represent the 50 percent confidence limits for a population of projectiles fired at a fixed target. In other words, if a number of shells were fired at a target, 50 percent of the shells would land in an ellipse centered on the target with a major radius equal to

*Swingle, D. M., unpublished work, US Army Atmospheric Sciences Laboratory, White Sands Missile Range, NM, 1979.

⁷Firing Tables, FT 155-AM-1, 1972, FT 8-J-4, 1967, Department of the Army, Washington, DC.

TABLE 1. BALLISTIC WIND COMPONENT VARIANCE (Kn^2) FOR AN AN/GMD-1 TRACKING SYSTEM

Ballistic Line Number	Balloon Ascent Rates		
	300 m/min	400 m/min	500 m/min
1	.047	.071	.101
2	.010	.009	.009
3	.016	.011	.009
4	.033	.022	.017
5	.163	.052	.038
6	.804	.071	.051
7	3.505	.219	.092
8	2.685	.549	.132
9	145.239	.773	.137
10	184.254	1.979	.216
11	212.168	3.149	.274
12	258.732	4.113	.419
13	255.730	2.366	.515
14	193.627	1.125	.424
15	142.338	1.031	.301

the range probable error and with a minor radius equal to the deflection probable error. Again, it should be pointed out that these probable errors are only the result of variability and measurement uncertainty of the met parameters; they do not represent errors due to lack of correction for the meteorology, variations in muzzle velocity, variations in angle of departure, etc.

RESULTS

Real meteorological sounding data, from Munich, Germany, in the early spring of 1976, were used for the probable error calculations. In calculating the probable errors, the numbers of possible combinations of range, weapon, charge, and balloon ascent rate are enormous. This problem was reduced to a manageable size by considering only some of the larger error cases. Since the unit effects increase with range, the tests made were for long ranges and larger charges for the 155-mm and 8-in weapon systems. It was also assumed that the target and gun were at the same altitude. For each range, a low and high trajectory test was conducted, showing the increased error when firing to a higher maximum ordinate. To demonstrate the effects of windspeed on the errors, data for several days of high winds (1 Jan and 21 Jan), low wind (8

Feb), and a baseline test with no wind were generated. All examples assumed a balloon ascent rate of 400 m/min. All of these assumptions seem realistic for a battlefield situation. Table 2 shows the firing scenarios for the eleven cases in which errors were calculated.

TABLE 2. FIRING SCENARIOS FOR THE MET DATA FREQUENCY STUDY

Case	Date (1976)	Time (LST)	Weapon	Charge	Range (km)	Trajectory		Ballistic	
						Max Ord (km)	Mean Wind (kn)	Wind (kn)	
1	21 Jan	1200	8 in	7	15	2.890	44.86	46.44	
2	21 Jan	1200	8 in	7	15	7.544	62.77	73.04	
3	21 Jan	1200	8 in	5	10	1.550	40.78	48.65	
4	21 Jan	1200	8 in	5	10	4.919	52.64	58.82	
5	21 Jan	1200	155 mm	8	16	3.056	45.21	52.14	
6	21 Jan	1200	155 mm	8	15	8.648	64.86	70.97	
7	21 Jan	1200	155 mm	6W	11	1.865	42.96	48.65	
8	21 Jan	1200	155 mm	6W	11	5.306	54.35	62.97	
9	Imaginary		8 in	7	12	1.445	0.00	0.00	
10	8 Feb	1200	8 in	7	12	1.445	2.87	3.28	
11	1 Jan	1200	8 in	7	12	1.445	44.12	46.25	

For each test the time staleness was varied from 0 to 360 min and the spacial staleness was varied from 0 to 60 km. The smaller values of staleness, while not realistic to the battlefield, show the amount of minimum error due to measurement uncertainty. A complete array of the probable errors for the entire spacial and temporal range mentioned above is given in tables in appendix A for all the cases listed in table 2.

Figure 1 shows range probable error versus time staleness for a constant spacial staleness of 20 km for cases 1 through 8 listed in table 2. As one would expect the larger errors occur for the longer ranges and higher winds because unit effects increase with range, and wind variability increases with windspeed. The lines in this figure are nearly straight, as one might expect from the linear relationship of time (in the space-time factor) to range variance in equation (1). The slope of the probable error curve is slightly larger at the low age end of the graph than for the high end, but the difference is small. Obviously, the optimum age for met data so far as accuracy is concerned will be as small as possible, since fresher met data will be used and met parameter variability will be reduced. However, the information in the figure is useful since the graph does quantify the error as a function of time lag. Another interesting feature of this graph is that

range probable error does not vanish even if there is no time separation between measurement and firing. Part of this error is due to the 20 km of spacial staleness in this example; the remaining amount of error is due to the measurement uncertainty of wind, temperature, and density.

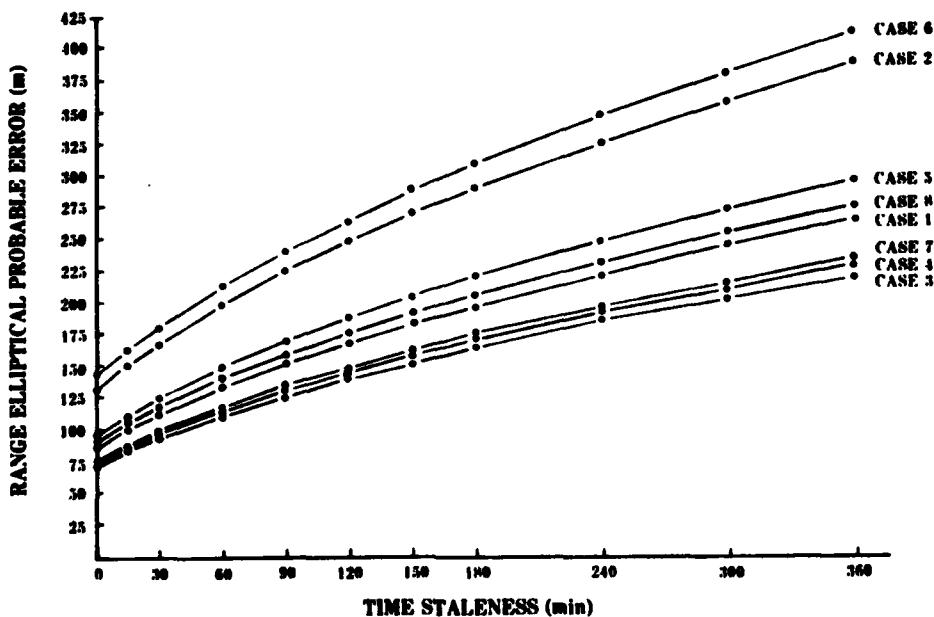


Figure 1. Range elliptical probable error versus time staleness while the spacial staleness was fixed at 20 km (cases 1 through 8).

Figure 2 shows deflection probable error versus time staleness for cases 1 through 8 in table 2. Again a spacial separation of 20 km was used. These errors are not as large as the range errors nor do they increase quite as rapidly with increasing temporal staleness, but similar to range error they do increase in a nearly linear manner. The main reason these deflection errors are smaller than the corresponding range errors is that the unit effects for the crosswind component of wind are quite a bit less than for the range wind component. Recall, too, that temperature and density effects were small for the deflection component and, consequently, were neglected.

The effect of spacial staleness on range probable error is shown in figure 3. For these examples the time staleness was fixed at 2 h while the spacial staleness was varied. Similar to figure 1, and for reasons previously discussed, the error increases with range and windspeed. These error curves are quite linear, but the dependence of the error on space is a little weaker than the dependence on time as shown in figure 1. The main reason for the weaker dependence is that in the space and time scales of the battlefield, the variability of wind in time is usually greater than in space. Recall that a 2-min change in time is approximately equivalent to a 1 km change in space. A typical met spacial staleness is about 25 km and a typical time staleness from measurement to use is about 3 h. Using the above rule the staleness owing to met spacing is 2 min/km times 25 km or 50 min, while the staleness owing to time is 180 min.

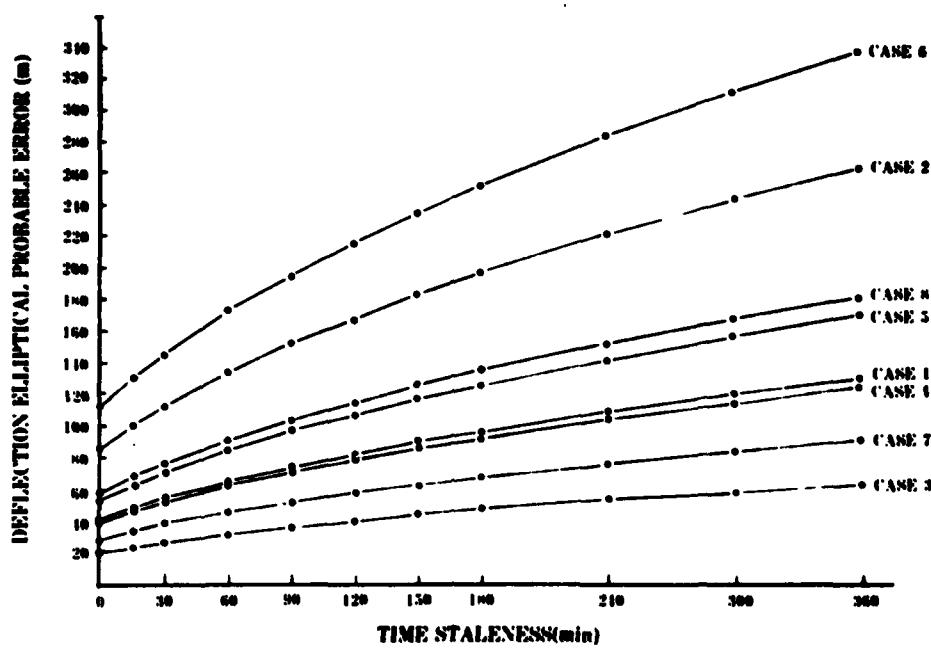


Figure 2. Deflection elliptical probable error versus time staleness while spacial staleness was fixed at 20 km (cases 1 through 8).

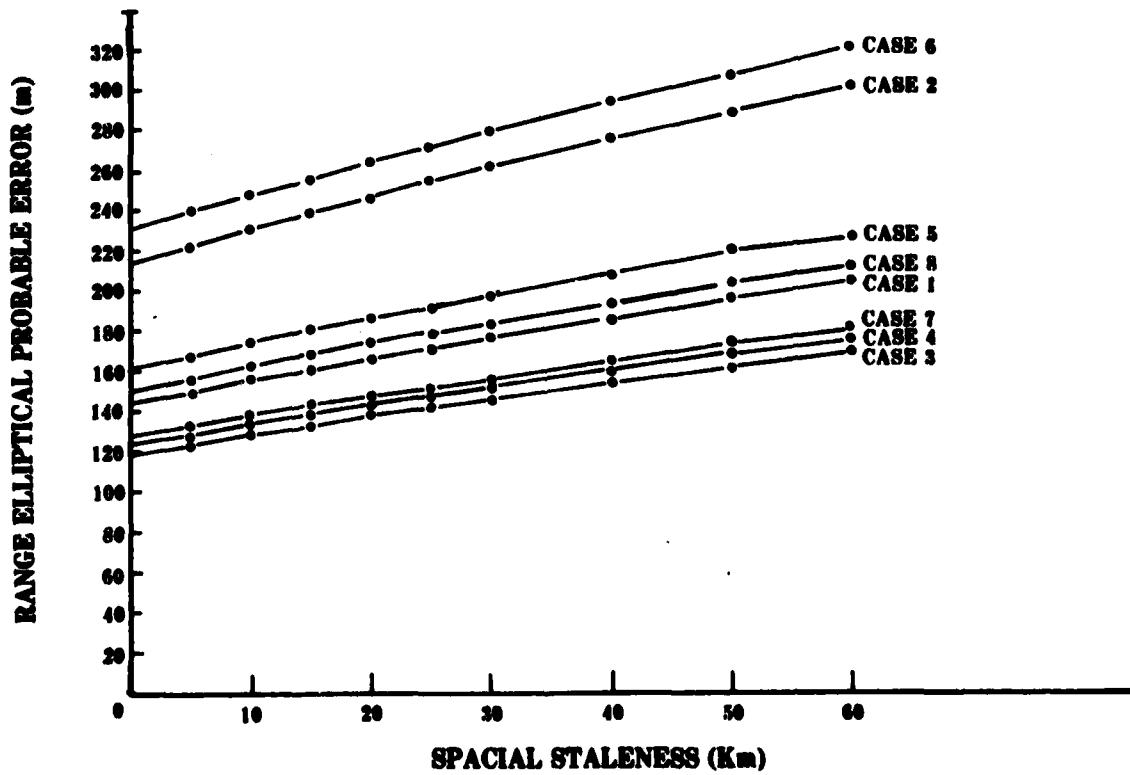


Figure 3. Range elliptical probable error versus spacial staleness while the time staleness was held at 2 h (cases 1 through 8).

Figure 4 is a graph of deflection probable error versus spacial staleness while the time lag was fixed at 2 h. The deflection probable errors are again less than the range probable errors. Also note that the slopes of the lines in figure 4 are not as large as those in figure 2 since met parameter variability in time is usually greater than in space.

To further access the effects of windspeed on probable error, several trials were conducted where ballistic windspeed ranged from moderate to an imaginary case with no wind while all other parameters, like range and quadrant elevation (QE), remained constant. The firing scenarios used were cases 9, 10, and 11 from table 2.

Figure 5 shows both the range and deflection probable error versus time staleness for a constant spacial staleness of 20 km. Again, errors increase with windspeed, the rate of error growth increases with speed, and errors do not disappear in the absence of wind since there is still a measurement uncertainty even when we have measured no wind. Also temperature and density contributions to the error are still left in the case of range probable error.

Figure 6 shows plots of probable error as a function of spacial staleness while the time lag was held at 2 h. The errors in this figure are linear with distance, and the size of the error is directly related to windspeed since all other met and firing conditions remain constant for these cases. Again the probable error rate of change in space is less than the change in time for the space and time scales in these examples.

Trying to separate the individual effects of wind, temperature, and density when viewing these graphs is quite difficult. To illustrate their effects, the individual range and deflection impact standard deviations as a function of space and time have been listed for cases 9 and 11 of table 2 in appendix A. Note that the errors due to measurement remain constant as time or space is varied. This occurs since the error is made at the time of measurement and does not depend on when the measured value is used. For a moderate ballistic wind, case 11, the errors due to met variability are dominant over the measurement errors with the range wind variability error being the largest. However, even with no wind as in case 9, the range wind variability is still the dominant error. This illustrates the importance of knowing the current wind no matter what its value. For these examples temperature and density variability and measurement errors were both important, but wind measurement error was quite small.

CONCLUSIONS

This study seems to reinforce what is already known: variability of ballistic wind is the largest source of met error for artillery weapons; but errors caused by temperature and density variation can make substantial contributions to the total error, especially when winds are light. The contribution to the total error because of wind measurement is highly dependent on balloon ascent rate and the ballistic zone to which measurements are made. Using a balloon with a 300 m/min ascent rate when making measurements above ballistic zone 8 can produce tremendous errors as seen by the measurement uncertainties listed in table 1. While the results of this study indicate what the optimum spacial and temporal frequency for obtaining met data is, as one would expect, as often as possible, the study is useful in quantifying errors that do exist. The user, then, can decide what trade-off is best for a particular battlefield situation.

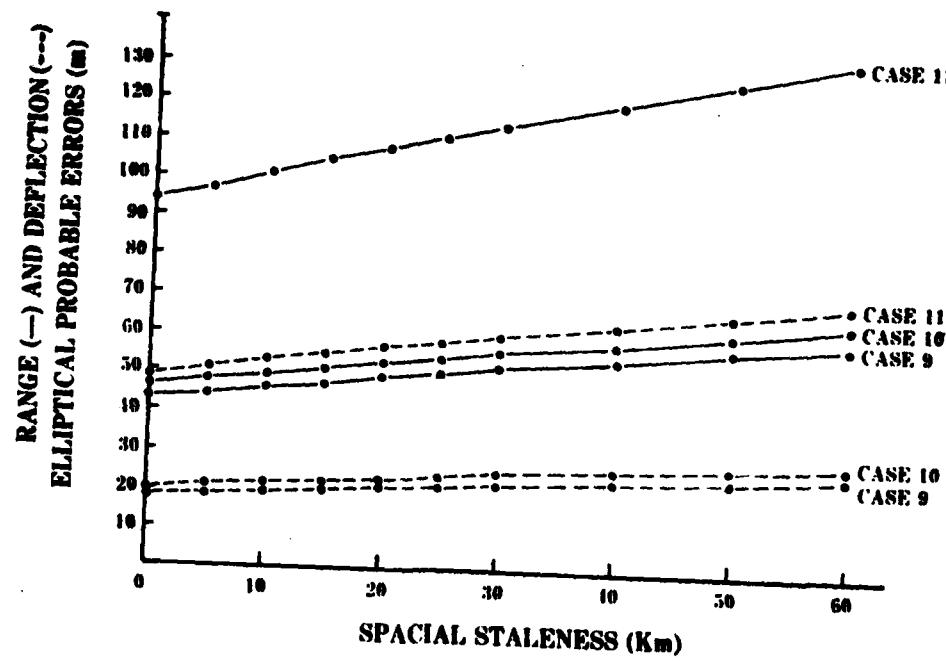


Figure 6. Range and deflection elliptical probable error versus spacial staleness while the time staleness was held at 2 h (cases 9 through 11).

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1. Lowenthal, M., and R. Bellucci, "Variability of Ballistic Winds," ECOM-3529, US Army Electronics Command, Fort Monmouth, NJ, 1970.
2. Durst, C. S., "The Variation of Wind with Time and Distance," Geophysical Memoir No 93, UK Meteorological Office, 1954.
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6. Engebos, Bernard F., "A Least Squares Approach to Missing Meteorological Data," ASL-CR-82-0008-1, US Army Atmospheric Sciences Laboratory, White Sands Missile Range, NM, 1982.
7. Firing Tables, FT 155-AM-1, 1972, FT 8-J-4, 1967, Department of the Army, Washington, DC.

APPENDIX A

Tables A-1 through A-11 present range and deflection elliptical probable errors as a function of spacial and temporal staleness for all cases listed in table 2 in the text. Tables A-12 through A-15 present the individual range and deflection impact standard deviations as a function of space and time staleness for cases 9 and 11 in table 2 in the text.

TABLE A-1. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON	WARHEAD	RANGE (KM)	QE (MILS)	CHARGE	MAX ORDINATE (KM)
M110A1 HOWITZER	M106	15.000	551.7	7	2.890
TIME STALENESS (MIN)	0	15	30	60	90
SPACE STALENESS (KM)	0	R 13	53	73	103
	D 3	25	35	50	61
	R 44	67	84	111	133
	D 21	32	41	54	64
	R 60	79	94	119	139
	D 29	38	46	58	68
	R 73	89	103	126	145
	D 35	43	50	61	71
	R 84	99	111	133	151
	D 41	48	54	64	73
	R 94	107	119	139	157
	D 46	52	58	68	76
	R 103	115	126	145	162
	D 50	56	61	71	79
	R 119	129	139	157	173
	D 58	63	68	76	84
	R 133	142	151	167	182
	D 64	69	73	81	89
	R 145	154	162	178	192
	D 71	75	79	86	93
	R 155	165	176	192	205
	D 79	83	87	96	106
	R 169	179	190	205	217
	D 84	88	92	104	115
	R 182	192	202	214	227
	D 91	95	104	117	127
	R 196	206	216	224	244
	D 97	101	110	119	129
	R 201	211	221	225	247
	D 100	108	110	120	130
	R 205	215	225	229	251
	D 100	111	111	122	132
	R 213	223	233	236	258
	D 104	115	115	125	135
	R 221	231	241	244	264
	D 102	112	112	122	132
	R 229	239	249	251	271
	D 106	116	122	132	141
	R 236	246	256	258	277
	D 108	118	128	138	148
	R 244	254	264	264	283
	D 110	120	130	140	150
	R 251	261	271	271	291
	D 111	121	131	141	151
	R 258	268	278	278	298
	D 115	125	135	145	155
	R 264	274	284	284	304
	D 119	129	139	149	159
	R 271	281	291	291	311
	D 122	132	142	152	162
	R 278	288	298	308	328
	D 125	135	145	155	165
	R 283	293	303	313	333
	D 129	139	149	159	179
	R 291	301	311	321	341
	D 132	142	152	162	182
	R 298	308	318	328	348
	D 135	145	155	165	185
	R 304	314	324	334	354
	D 138	148	158	168	188
	R 311	321	331	341	361
	D 141	151	161	171	191
	R 318	328	338	348	368
	D 144	154	164	174	194
	R 324	334	344	354	374
	D 147	157	167	177	197
	R 331	341	351	361	381
	D 150	160	170	180	200
	R 338	348	358	368	388
	D 153	163	173	183	203
	R 344	354	364	374	394
	D 156	166	176	186	206
	R 351	361	371	381	401
	D 159	169	179	189	209
	R 358	368	378	388	408
	D 162	172	182	192	212
	R 364	374	384	394	414
	D 165	175	185	195	215
	R 371	381	391	401	421
	D 168	178	188	198	218
	R 378	388	398	408	428
	D 171	181	191	201	221
	R 384	394	404	414	434
	D 174	184	194	204	224
	R 391	401	411	421	441
	D 177	187	197	207	227
	R 398	408	418	428	448
	D 180	190	200	210	230
	R 404	414	424	434	454
	D 183	193	203	213	233
	R 411	421	431	441	461
	D 186	196	206	216	236
	R 418	428	438	448	468
	D 189	199	209	219	239
	R 424	434	444	454	474
	D 192	202	212	222	242
	R 431	441	451	461	481
	D 195	205	215	225	245
	R 438	448	458	468	488
	D 198	208	218	228	248
	R 444	454	464	474	494
	D 201	211	221	231	251
	R 451	461	471	481	501
	D 204	214	224	234	254
	R 458	468	478	488	508
	D 207	217	227	237	257
	R 464	474	484	494	514
	D 210	220	230	240	260
	R 471	481	491	501	521
	D 213	223	233	243	263
	R 478	488	498	508	528
	D 216	226	236	246	266
	R 484	494	504	514	534
	D 219	229	239	249	269
	R 491	501	511	521	541
	D 222	232	242	252	272
	R 498	508	518	528	548
	D 225	235	245	255	275
	R 504	514	524	534	554
	D 228	238	248	258	278
	R 511	521	531	541	561
	D 231	241	251	261	281
	R 518	528	538	548	568
	D 234	244	254	264	284
	R 524	534	544	554	574
	D 237	247	257	267	287
	R 531	541	551	561	581
	D 240	250	260	270	290
	R 538	548	558	568	588
	D 243	253	263	273	293
	R 544	554	564	574	594
	D 246	256	266	276	296
	R 551	561	571	581	591
	D 249	259	269	279	299
	R 558	568	578	588	598
	D 252	262	272	282	302
	R 564	574	584	594	604
	D 255	265	275	285	305
	R 571	581	591	601	611
	D 258	268	278	288	308
	R 578	588	598	608	618
	D 261	271	281	291	311
	R 584	594	604	614	624
	D 264	274	284	294	314
	R 591	601	611	621	631
	D 267	277	287	297	317
	R 598	608	618	628	638
	D 270	280	290	300	320
	R 604	614	624	634	644
	D 273	283	293	303	323
	R 611	621	631	641	651
	D 276	286	296	306	326
	R 618	628	638	648	658
	D 279	289	299	309	329
	R 624	634	644	654	664
	D 282	292	302	312	332
	R 631	641	651	661	671
	D 285	295	305	315	335
	R 638	648	658	668	678
	D 288	298	308	318	338
	R 644	654	664	674	684
	D 291	301	311	321	341
	R 651	661	671	681	691
	D 294	304	314	324	344
	R 658	668	678	688	698
	D 297	307	317	327	347
	R 664	674	684	694	704
	D 300	310	320	330	350
	R 671	681	691	701	711
	D 303	313	323	333	353
	R 678	688	698	708	718
	D 306	316	326	336	356
	R 684	694	704	714	724
	D 309	319	329	339	359
	R 691	701	711	721	731
	D 312	322	332	342	362
	R 698	708	718	728	738
	D 315	325	335	345	365
	R 704	714	724	734	744
	D 318	328	338	348	368
	R 711	721	731	741	751
	D 321	331	341	351	371
	R 718	728	738	748	758
	D 324	334	344	354	374
	R 724	734	744	754	764
	D 327	337	347	357	377
	R 731	741	751	761	771
	D 330	340	350	360	380
	R 738	748	758	768	778
	D 333	343	353	363	383
	R 744	754	764	774	784
	D 336	346	356	366	386
	R 751	761	771	781	791
	D 339	349	359	369	389
	R 758	768	778	788	798
	D 342	352	362	372	392
	R 764	774	784	794	804
	D 345	355	365	375	395
	R 771	781	791	801	811
	D 348	358	368	378	398
	R 778	788	798	808	818
	D 351	361	371	381	401
	R 784	794	804	814	824
	D 354	364	374	384	404
	R 791	801	811	821	831
	D 357	367	377	387	407
	R 798	808	818	828	838
	D 360	370	380	390	410
	R 804	814	824	834	844
	D 363	373	383	393	413
	R 811	821	831	841	851
	D 366	376	386	396	416
	R 818	828	838	848	858
	D 369	379	389	399	419
	R 824	834	844	854	864
	D 372	382	392	402	422
	R 831	841	851	861	871
	D 375	385	395	405	425
	R 838	848	858	868	878
	D 378	388	398	408	428
	R 844	854	864	874	884
	D 381	391	401	411	431
	R 851	86			

TABLE A-2. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON M110A1 HOWITZER	WARHEAD M106	RANGE (KM) 15.000	OE (MILES) 1060.2	CHARGE 7	MAX ORDINATE (KM) 7.544
TIME STALENESS(MIN)	0	15	30	60	90
SPACE STALENESS(KM)	R 40	85	113	155	188
0	D 24	56	75	104	126
				145	162
5	R 73	105	129	167	198
	D 48	70	86	112	133
				151	167
10	R 95	121	143	178	207
	D 63	81	95	119	139
				156	172
15	R 113	136	155	186	216
	D 75	91	104	126	145
				162	177
20	R 129	149	167	198	224
	D 86	100	112	133	151
				167	182
25	R 143	161	178	207	232
	D 95	108	119	139	156
				172	186
30	R 155	172	188	216	240
	D 104	116	126	145	162
				177	191
40	R 178	193	207	232	256
	D 119	130	139	156	172
				186	199
50	R 198	211	224	248	270
	D 133	142	151	167	182
				195	208
60	R 216	228	240	263	283
	D 145	154	162	177	191
				204	216
				227	249
				239	259
				250	270
				262	282
				274	294
				285	305
				296	316
				307	327
				318	338
				329	349
				340	360
				351	371
				362	382
				373	393
				384	404
				395	415
				406	426
				417	437
				428	448
				439	459
				450	470
				461	481
				472	492
				483	503
				494	514
				505	525
				516	536
				527	547
				538	558
				549	569
				560	580
				571	591
				582	602
				593	613
				604	624
				615	635
				626	646
				637	657
				648	668
				659	679
				670	690
				681	701
				692	712
				703	723
				714	734
				725	745
				736	756
				747	767
				758	778
				769	789
				780	800
				791	811
				802	822
				813	833
				824	844
				835	855
				846	866
				857	877
				868	888
				879	899
				890	910
				901	921
				912	932
				923	943
				934	954
				945	965
				956	976
				967	987
				978	998
				989	1009
				990	1010
				1001	1021
				1012	1032
				1023	1043
				1034	1054
				1045	1065
				1056	1076
				1067	1087
				1078	1098
				1089	1109
				1090	1110
				1101	1121
				1112	1132
				1123	1143
				1134	1154
				1145	1165
				1156	1176
				1167	1187
				1178	1198
				1189	1209
				1190	1210
				1201	1221
				1212	1232
				1223	1243
				1234	1254
				1245	1265
				1256	1276
				1267	1287
				1278	1298
				1289	1309
				1290	1310
				1301	1321
				1312	1332
				1323	1343
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				1356	1376
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				1378	1398
				1389	1409
				1390	1410
				1401	1421
				1412	1432
				1423	1443
				1434	1454
				1445	1465
				1456	1476
				1467	1487
				1478	1498
				1489	1509
				1490	1510
				1501	1521
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				1545	1565
				1556	1576
				1567	1587
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				1589	1609
				1590	1610
				1601	1621
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				1690	1710
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				1745	1765
				1756	1776
				1767	1787
				1778	1798
				1789	1809
				1790	1810
				1801	1821
				1812	1832
				1823	1843
				1834	1854
				1845	1865
				1856	1876
				1867	1887
				1878	1898
				1889	1909
				1890	1910
				1901	1921
				1912	1932
				1923	1943
				1934	1954
				1945	1965
				1956	1976
				1967	1987
				1978	1998
				1989	2009
				1990	2010
				2001	2021
				2012	2032
				2023	2043
				2034	2054
				2045	2065
				2056	2076
				2067	2087
				2078	2098
				2089	2109
				2090	2110
				2101	2121
				2112	2132
				2123	2143
				2134	2154
				2145	2165
				2156	2176
				2167	2187
				2178	2198
				2189	2209
				2190	2210
				2201	2221
				2212	2232
				2223	2243
				2234	2254
				2245	2265
				2256	2276
				2267	2287
				2278	2298
				2289	2309
				2290	2310
				2301	2321
				2312	2332
				2323	2343
				2334	2354
				2345	2365
				2356	2376
				2367	2387
				2378	2398
				2389	2409
				2390	2410
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				2456	2476
				2467	2487
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				2489	2509
				2490	2510
				2501	2521
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				2556	2576
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				2745	2765
				2756	2776
				2767	2787
				2778	2798
				2789	2809
				2790	2810
				2801	2821
</					

TABLE A-3. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON	WARHEAD	RANGE (KM)	DE (MILS)	CHARGE	MAX ORDINATE (KM)
M110A1 HOWITZER	M106	10.000	512.4	5	1.550
TIME STALENESS (MIN)	0	15	30	60	70
SPACE STALENESS (KM)	R	43	60	85	104
0	D	12	17	24	29
5	R	35	55	70	92
	D	10	15	20	26
10	R	49	65	78	98
	D	14	18	22	28
15	R	60	74	85	104
	D	17	21	24	29
20	R	70	82	92	110
	D	20	23	26	31
25	R	78	89	98	115
	D	22	25	28	32
30	R	85	95	104	120
	D	24	27	29	34
40	R	98	107	115	130
	D	28	30	32	36
50	R	110	118	125	139
	D	31	33	35	39
60	R	120	128	134	147
	D	34	36	38	41
WEAPON		48-65	WD MSMT UNC (KT ²)	052	NO BOMBLETS
WEAPON		400	AR (M/MIN)	400	

TABLE A-4. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON M110A1 HOWITZER		WARHEAD M106	RANGE (KM) 10.000	WE (MILS) 1078.4	CHARGE 5	MAX ORDINATE (KM) 4.919	
TIME STALENESS (MIN)	0	15	30	60	90	120	150
SPACE STALENESS (KM)	0	R 13	46	64	89	109	126
	D 7	25	34	48	59	68	75
	R 38	59	73	96	115	131	140
	D 21	31	39	52	62	70	78
	R 53	69	82	103	120	136	149
	D 28	37	44	55	65	73	80
	R 64	78	89	109	126	140	154
	D 34	42	48	59	68	75	83
	R 73	86	96	115	131	145	158
	D 39	46	52	62	70	78	85
	R 82	93	103	120	136	149	162
	D 44	50	55	65	73	80	87
	R 89	100	109	126	140	154	166
	D 48	54	59	68	75	83	89
	R 103	112	120	136	149	162	174
	D 55	60	65	73	80	87	93
	R 115	123	131	145	158	170	181
	D 62	66	70	78	85	91	97
	R 126	133	140	154	166	177	188
	D 68	72	75	83	89	95	101
BALL. WIND (KT)		WD	MSMT	UNC (KT ²)	AR (M/MIN)		
58.82		.549			400 NO BOMBLETS		

TABLE A-5. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON	WARHEAD	RANGE (KM)	DE (MILS)	CHARGE 8	MAX ORDINATE (KM)
M109A1 HOWITZER	M107	16.000	518.6		3.056
TIME STALENESS (MIN)	0	15	30	90	240
SPACE STALENESS (KM)	0	R 21	61	84	229
	D 6	33	46	141	256
	R 51	77	96	125	145
	D 27	42	53	149	159
	R 69	90	106	134	161
	D 38	50	60	156	164
	R 84	101	116	141	164
	D 46	56	65	163	165
	R 96	111	125	149	165
	D 53	62	70	169	168
	R 106	121	134	156	168
	D 60	68	75	176	170
	R 116	129	141	163	170
	D 65	73	80	182	170
	R 134	145	156	176	172
	D 75	82	98	193	176
	R 149	160	169	188	176
	D 84	90	96	204	176
	R 163	173	182	199	176
	D 92	97	103	142	176
WEAPON	BALL. WIND (KT)	WD MSMT UNC (KT^2)	AR (M/MIN)		
52.14	.219	NO BOMBLETS	.400		

TABLE A-7. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON M109A1 HOWITZER		WARHEAD M107	RANGE (KM) 11.000	OE (MILS) 526.8	CHARGE 6	MAX ORDINATE (KM) 1.865
TIME STALENESS (MIN)	0	15	30	60	90	120
SPACE STALENESS (KM)	0	R 7	46	65	91	111
	D 2	17	25	35	43	49
5	R 38	59	74	98	117	134
	D 14	22	28	38	45	51
10	R 53	70	83	105	123	139
	D 20	27	32	40	47	53
15	R 65	79	91	111	129	144
	D 25	30	35	43	49	55
20	R 74	87	98	117	134	148
	D 28	33	38	45	51	57
25	R 83	95	105	123	139	153
	D 32	36	40	47	53	58
30	R 91	102	111	129	144	157
	D 35	39	43	49	55	60
40	R 105	114	123	139	153	166
	D 40	44	47	53	58	63
50	R 117	126	134	148	162	174
	D 45	48	51	57	62	66
60	R 129	136	144	157	170	182
	D 49	52	55	60	65	69
WEAPON 48.65		WD MSMT VNC (KT ^{1/2}) .052	ARC/MIN) 400	NO BOMBLETS		

TABLE A-8. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON	WARHEAD	RANGE (KM)	WE (MILS)	CHARGE	MAX ORDINATE (KM)
	M109A1 HOWITZER	11.000	1049.7	6	5.306
TIME STALENESS (MIN)	0	15	30	60	90
SPACE STALENESS (KM)	0	R 19	56	70	100
	D 11	37	50	70	96
5	R 47	71	84	117	139
	D 31	46	58	76	90
10	R 64	83	99	124	145
	D 42	54	64	81	95
15	R 78	94	106	132	152
	D 50	61	70	86	99
20	R 89	104	117	139	158
	D 58	68	76	90	103
25	R 99	112	124	145	164
	D 64	73	81	95	107
30	R 108	121	132	152	169
	D 70	77	86	99	111
40	R 124	135	145	164	180
	D 81	88	95	107	118
50	R 139	149	158	175	190
	D 90	97	103	114	124
60	R 152	161	169	185	200
	D 99	105	111	121	131
WEAPON		BALL. WIND (KT)	WD MSMT UNC (KT ²)	AK (M/MIN)	NO BOMBLETS
		62.97	.773	.400	

TABLE A-9. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON M110A1 HOWITZER	WARHEAD M106	RANGE (KM) 12.000	QE (MILS) 360.1	CHARGE 7	MAX ORDINATE (KM) 1.445
TIME STALENESS (MIN)	0	15	30	60	90
SPACE STALENESS (KM)	0	13	19	24	32
	R	1	6	9	13
	D	1	6	10	14
	R	17	23	27	34
	D	5	8	10	14
	R	21	26	29	36
	D	7	10	12	15
	R	24	28	32	38
	D	9	11	13	16
	R	27	31	34	39
	D	10	12	14	16
	R	29	33	36	41
	D	12	13	15	17
	R	32	35	38	43
	D	13	14	16	18
	R	36	39	41	46
	D	15	16	17	19
	R	39	42	44	49
	D	16	18	19	21
	R	43	45	47	52
	D	18	19	20	22
WEAPON	BALL, WIND (KT)	WD MSMT	VNC (KT^2)	AR (M/MIN)	NO BOMBLETS
	0.00	.022	.022	400	

TABLE A-11. RANGE AND DEFLECTION ELLIPTICAL PROBABLE ERRORS (METERS)

WEAPON	WARHEAD	RANGE (KM)	DE (MILS)	CHARGE	MAX ORDINATE (KM)
M110A1 HOWITZER	M106	12,000	360.1	7	1,445
TIME STALENESS (MIN)	0	15	30	60	90
SPACE STALENESS (KM)	0	R 13 D 1	35 17	48 25	67 42
					81 49
					94 51
					97 57
					108 62
					117 71
					135 79
					150 79
					147 77
					147 85
5	R 30 D 14	44	55	72	86
					45
					51
					57
					62
					71
10	R 40 D 20	52	64	77	90
					47
					53
					58
					63
					72
15	R 48 D 25	58	67	81	94
					49
					55
					60
					65
					73
					81
					88
20	R 55 D 28	64	72	86	97
					45
					51
					57
					62
					66
					75
					82
					89
25	R 61 D 32	70	77	90	101
					47
					53
					58
					63
					68
					76
					84
					91
30	R 67 D 35	74	81	94	105
					42
					49
					53
					58
					63
					68
					72
					77
					85
					92
40	R 77 D 40	84	90	101	111
					47
					49
					53
					58
					63
					68
					72
					77
					80
					87
					94
50	R 86 D 45	92	97	108	117
					51
					57
					62
					66
					71
					75
					82
					89
					96
60	R 94 D 49	99	105	114	123
					52
					55
					60
					65
					69
					73
					77
					85
					92
					99
BALL. WIND (KT)			WD MSMT	UNC (KT ²)	AIR (M/MIN)
46.25			.022	400	NO BOMBLETS
WEAPON					

TABLE A-12. IMPACT RANGE AND DEFLECTION STANDARD DEVIATIONS (METERS)

WEAPON	WARTHED M106	RANGE(KM) 12.000	WE(MILES) 360.1	CHARGE 7	MAX ORDNINATE (KM) 1.445
TIME STALENESS(MIN)	0	15	30	60	70
RG WD VRBLTY	16	19	21	25	29
RG WD MSMT	1.66	1.66	1.66	1.66	1.66
RG TD VRBLTY	12	14	16	19	22
RG TD MSMT	11	11	11	11	11
DFL WD VRBLTY	9	10	12	14	16
DFL WD MSMT	.91	.91	.91	.91	.91
WEAPON NO BOMBLETS	BALL. WIND(kt) 0.00	SPACIAL STALENESS(KM) 20.00	AK(M/MIN) 4.00		

TABLE A-13. IMPACT RANGE AND DEFLECTION STANDARD DEVIATIONS (METERS)

WEAPON	WARHEAD	RANGE (KM)	DE (MILES)	CHARGE	MAX. ORDNATE (KN)
M110A1 HOWITZER	M106	12.000	360.1	7	1.445
TIME STALENESS (MIN)	0	15	30	60	90
RG WD URBLY	44	51	53	69	79
RG WD MSMT	1.66	1.66	1.66	1.66	1.66
RG TD URBLY	12	14	16	19	22
RG TD MSMT	11	11	11	11	11
DFL WD URBLY	24	28	32	38	43
DFL WD MSMT	.91	.91	.91	.91	.91
WEAPON	BALL. WIND (KT)	SPACIAL	STALENESS (KM)	AK (M/MIN)	
NO BOMBLETS	46.25	20.00	400		

TABLE A-14. IMPACT RANGE AND DEFLECTION STANDARD DEVIATIONS (METERS)

WEAPON	WARHEAD	RANGE (KM)	DE (MILES)	CHARGE	MAX ORDINATE (KM)
M110A1 HOWITZER	M106	12.000	360.4	7	1.44 _b
SPACE STALENESS (KM)	0	5	10	20	30
RG WD VRLTY	28	29	30	31	32
RG WD MSMT	1.66	1.66	1.66	1.66	1.66
RG TD VRLTY	21	22	22	23	24
RG TD MSMT	11	11	11	11	11
DFL WD VRLTY	15	16	16	17	18
DFL WD MSMT	.71	.71	.71	.71	.71
BALL. WIND (KT)		TIME STALENESS (MIN)		AK (M/MIN)	
WEAPON	0.00	120	400		
NO BOMBLETS					

TABLE A-15. IMPACT RANGE AND DEFLECTION STANDARD DEVIATIONS (METERS)

WEAPON	WARHEAD M110A1 HOWITZER	RANGE(KM) 12.000	OE(MILES) 360.4	CHARGE 7	MAX ORDINATE (KM) 1.445
SPACE STALENESS(KM)	0	5	10	20	30
RC WD VRBLTY	76	79	82	85	88
RC WD MSHT	1.66	1.66	1.66	1.66	1.66
RC TD VRBLTY	21	22	22	23	24
RC TD MSHT	11	11	11	11	11
DFL WD VRBLTY	42	43	45	47	48
DFL WD MSHT	.91	.91	.91	.91	.91
WEAPON	BALL. WIND(KT) 46.25	TIME STALENESS(MIN) 120	AK(M/MIN) 400		
NO BOMBLETS					

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